Challenge Question 2

MATH 1850 - Linear Algebra for Engineers $17~{\rm May}~2024$

Recall that a matrix A is called **symmetric** if $A = A^{\top}$. Similarly, a matrix A is called **skew-symmetric** if $A = -A^{\top}$. Prove that every square matrix A can be expressed as the sum of a symmetric matrix and a skew-symmetric matrix. (Hint: You may use the identity $A = \frac{1}{2}(A + A^{\top}) + \frac{1}{2}(A - A^{\top})$, but you need to prove it first!).